

A hybrid algorithm for parameter estimation of the short-ghrelin dynamics

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ABSTRACT

Food intake, bodyweight and appetite are controlled by a “web of hormones.” Recently, from this aforementioned web of hormones, several hormones have been revealed and investigated from a medical standpoint with different degrees of success: a key one is ghrelin. Accordingly, ghrelin is an orexigenic (i.e., appetite stimulant) hormone; in fact, the only one of its kind, a peripheral hormone that can influence, centrally, one’s propensity to start a meal. On this work, we shall present a problem in parameter estimation using evolutionary algorithms in conjunction with local search, what we have called herein hybrid algorithms (global search + local search); additionally, we apply artificial neural networks (feedforward neural network) for supporting the numerical simulations (what we have named “fake data”). Moreover, we present a mathematical model for ghrelin partially published elsewhere by the same authors; in addition, we have confronted the model mathematically with in vivo data via parameter estimation (well-known as validation) and got promising results for the novel mathematical formulation for ghrelin dynamics. Thus, our aim is showing that our algorithms can be imperative for fitting the current and future versions of the model. Notwithstanding the parameter estimation was unable to model precisely the experimental data, most likely due to physiological details still unclear in the medical literature, it generated an optimized curve relatively close to the experimental data, leaving promising results for future investigations.

Keywords: Ghrelin, Parameter Estimation, Evolutionary Computing. Artificial Neural Networks; Food Intake and Appetite Control.

I INTRODUCTION

Food intake, bodyweight and appetite are controlled by a “web of hormones” [1]. Those hormones may play similar/equal role, or quite diverse ones, but in the overall their actions emerge towards a common physiological role to make possible the precise control of bodyweight (energy homeostasis) that can be seen in most living systems (e.g., humans). Accordingly, the workings of this web of hormones culminate in food intake/appetite control (i.e., energy input). How the human body accomplishes bodyweight and food intake control precisely is still an ongoing research (the details of the physiological process), notwithstanding it has been done substantial progress in the last decades by unveiling key hormones such as ghrelin, leptin, and insulin; three key players on food intake and energy homeostasis control.

Ghrelin is an orexigenic (i.e., appetite stimulant) hormone [3-5]; in fact, the only one of its kind, a peripheral hormone that can influence centrally one’s propensity to start a meal [3]; its effect seems to be mediated by a group of neurons in the brain (arcuate nucleus) [6]. This group of neurons is the same aimed by

leptin and insulin, mediated for releasing neuropeptide γ . Ghrelin was found to be influenced by or/and influence key hormones, e.g. leptin and insulin, which may operate in different time-scales. Additionally, ghrelin is a short-time scale hormone – it operates in hours, it is said to increase about 1-2 hours before each meal, and to fall off about 1 hours after a meal has been terminated [3] – . The fall-off of ghrelin concentrations in blood-stream as a consequence of meals is a function of some factors such as macronutrients present in the foodstuff (e.g., carbohydrates) [7]. Our main aim is showing that our algorithms, based on hybrid algorithms instead of plain search, can be imperative for fitting the current and future versions of the model (future versions of the model might get much more complicate due to hormone/factor interconnectivity [1]) to experimental data, and we get it by the numerical results (Fig. 2)¹. As we shall see, our optimization problem, eq. 8, is a residual error function that should be minimized, employed for measuring how well or badly is our model performing when compared to experimental data, called parameter estimation/system identification [2]. Our

¹ A new version has been worked out by [18] and coworkers. They have achieved nice results by adding insulin and GLP-1 to the system.

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hypothesis is that our model, see for more [1,4] discussions, can be used to explain experimental data, collected by independent group, in vivo data, from human. And we succeed at a first stage, as can be seen in the simulation section.

On this work, we shall present a problem in parameter estimation using evolutionary algorithms alongside local search, what we have called hybrid algorithms (global search + local search, Fig. 3); furthermore, we apply artificial neural networks for supporting the numerical simulations. The work is based on Pires (2017) [1] and Pires et al (2017) [4].

1.1 ORGANIZATION OF THE WORK

In the next section, Mathematical Formulation, we present the model per se, the mathematical formulation in detail. In the following section, Parameter Estimation, we take the model presented previously and confront it with experimental data (*in vivo* vs. *in silico*). In the section following, Discussions, we add something more to the model, such as future works. Finally, we close the paper with a brief section, Final Remarks. We provide the reader with a concise set of references following the Final Remarks.

II MATHEMATICAL FORMULATION

On this section, we shall present and discuss on a ghrelin model/dynamics based on insights already discussed somewhere else by the same authors [1-4], with gastric emptying rate feedback (the gastric emptying rate was added to the model in an at-tempt to respond to some literatures (e.g., [16]) pinning down this imperative physio-logical detail); then, we shift to parameter estimation (which is an independent section).

1.1 EQUATIONS

The first equation is for the stomach, eq.1. The equation is a classical “input-output” (deterministic) differential equation, which can be encountered in most books in ordinary differential equations. Accordingly, eq.1 aims at modeling the dynamics of in-put-output that occurs in the stomach as a consequence of foodstuff intake (based on mass conservation). The equation is composed of an input term, i.e. foodstuff from mouth to stomach, and a second term from stomach to small intestine (called chyme). Notwithstanding the small intestine is composed of three-anatomical segments (duodenum, jejunum, and ileum), we shall not model them in detail; details may be needed in future models omitted herein since several literatures found that the control of ghrelin production seems to be physically located between the duodenum and jejunum (the middle and last section of the small intestine).

$$\frac{dS(t)}{dt} = F(t) - f_1(D(t))S(t) \tag{1}$$

We have, as a direct consequence of eq.1, the following equations: i) eq.2 is for food intake (F(t)); ii) eq.3 is for modeling gastric emptying feedback (f1(D(t)S(t))). Eq.2 is a simple degree/step function, it takes a constant value within an interval of time (i.e., lunch time, represented by τ in the equation), and zero otherwise (outside the interval of time $t + \tau$). Of course, this function is not completely physiologically plausible because one eats in a more complex manner; this constant value can be seen as an average for the whole interval. Eq.3 is a function for

controlling the output of the stomach (pylorus) based on excitation of the small intestine (represented by the letter D).

$$F(t) = \begin{cases} r, & \text{if } t \in [t_b, t_b + \tau_b] \\ r, & \text{if } t \in [t_l, t_l + \tau_l] \\ r, & \text{if } t \in [t_d, t_d + \tau_d] \\ 0, & \text{elsewhere} \end{cases} \tag{2}$$

$$f_1(D(t)) = \frac{k_{SD}}{1 + \delta D(t)} \tag{3}$$

In the upcoming tables (Table 1 and Table 2), we have organized the states variables and parameters of the model.

Table 1: State variables.

State Variable	Meaning in the model	Group
S(t)	Stomach, amount of foodstuff in the stomach in kcal	Gastrointestinal tract
D(t)	Small intestine, amount of food in the small intestine in kcal	
G(t)	Ghrelin, amount of ghrelin in bloodstream, in pg/ml	

Source: Authors, (2018).

Table 2: Parameters.

Parameter	Meaning in the model	Type	Group
r	Rate of food intake, kcal/min	FF	Meal
t _b	Time when one initiates a breakfast, h	FL	
t _l	Time when one initiates lunch, h	FL	
t _d	Time when one initiates dinner, h	FL	
τ _l	Duration of lunch, min	ES	
τ _d	Duration of dinner, min	ES	
τ _b	Duration of breakfast, min	ES	
k _{SD}	Flux of matter (chyme) from stomach to small intestine, transference rate, h ⁻¹	FF	Gastrointestinal tract
δ	Gastric emptying feedback, controlled by the small intestine, kcal ⁻¹	ES	
k _{DX}	Foodstuff, now processed by the stomach and small intestine, is eliminated on this rate, h ⁻¹	FF	
k _{HX}	Ghrelin elimination rate from bloodstream, first-order elimination rate, h ⁻¹	FF	
γ	Scaling parameter how the small intestine influences the production of ghrelin negatively, suppression, kcal ⁻¹	ES	

Legend. FF – Fixed values, set by the modeler, without any strong reason; FL – fixed from literature, that is, from publication; ES – estimated, using parameter estimation.

Source: Authors, (2018).

One important (modeling) detail about eq.3 is that it does not model the true physiological phenomenon (see Fig. 1), the feedback from the small intestine into gastric emptying rate. Consequently, eq.3 it models a surrogate variable herein called small intestine (D). The rationale behind this modeling simplification is that the hormones that truly participate in the dynamics of controlling the gastric emptying feedback are all produced directly/indirectly proportionally to the amount of nutrient load in the small intestine, as so, being the amount of food in the small intestine as we are methodologically accepting a pretty good approximation.

Next equations are: i) small intestine, eq.4; and ii) ghrelin dynamics, eq. 5. As a direct consequence of eq.6, we have eq.7. Eq.7 was created to account for the shift in dynamics between day and night behavior of ghrelin (around $t = 25h = 2 \text{ am}$ [3]), it was observed in the literature [3]; however, a plausible physiological explanation has not been yet published to the best of our knowledge, and eq.7 is the most naïve way to handle the issue mathematically.

$$\frac{dD(t)}{dt} = f_1(D(t))S(t) - k_{DX}D(t) \quad (4)$$

$$\frac{dH(t)}{dt} = f_2(D(t)) - k_{HX}H(t) \quad (5)$$

As a direct consequence of eq.5, we have:

$$f_2(D(t)) = \frac{\beta}{1 + \gamma D(t)} \quad (6)$$

$$\beta = \begin{cases} \beta_d, & t \leq t_{switch} \\ \beta_n, & t > t_{switch} \end{cases} \quad (7)$$

In the upcoming figure, Fig. 1, we have a scheme of the gastric emptying feed-back: as the small intestine is loaded with (processed) foodstuff, the more hormones are produced; and the more hormones are produced, the higher is the suppression effect; one exception omitted is ghrelin, which induces gastric emptying, in the scheme we should have for ghrelin an arrow-headed vector instead of bar-headed vector (which means suppression).

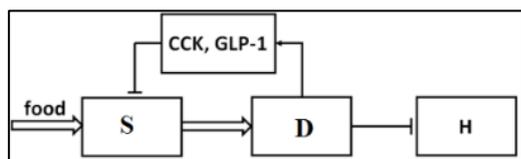


Figure 1: Gastric emptying feedback system.
Source: adapted from Pires et al [3].

Table 3: List of equations.

Eq.	Meaning in the model	Group
1	Stomach dynamics – on this equation, one can find a mathematical description of the dynamics happening in the stomach, foodstuff comes in and chyme comes out; a mass conservation formulation.	Gastrointestinal tract
2	Food intake – this equation models the food intake as an “on-off function”	
3	Gastric feedback – this equation describes the feedback created by the small intestine in the stomach output.	
4	Small intestine dynamics – as foodstuff leaves the stomach as chyme, this equation models the dynamics of input-output	
5	Ghrelin equation – this equation represents how ghrelin changes as a function of time, in the bloodstream in terms of concentration, pg/(ml*min)	Ghrelin dynamics
6	Ghrelin production dynamics – this equation models how ghrelin production changes as a function of time, pg/(min*ml)	
7	Diurnal-nocturnal production rate of ghrelin – ghrelin was found to have a shift in dynamics during sleep-time, a nocturnal dynamics most likely caused by several hormones produced during the night	

Source: Authors, (2018).

III PARAMETER ESTIMATION

III.1 THEORETICAL CONSIDERATIONS

Fitness/loss function. The fitness or loss function is a mathematical relation used to measure how well/badly an algorithm/model is performing on its task [8]; it is minimized for finding the best parameters of a model. Thus, for having a fitness function we need to have a way of measuring what we want; i.e. a measure of distance from “bad to good.” Once we have this measure, we just need to minimize/maximize this relationship; in biology, that may become problematic since not always the optimal is what we can find in real physiological systems, and such an approach is merely a mathematical trick. The optimal parameters found by an algorithm may not be necessarily physiologically plausible, or the one actually tuned by evolution.

The commonest function is called Residual Sum of Squares (RSS), also known as the Sum of Squared Residuals/ Sum of Squares Residuals (SSR) [8]. In one of its variations, it is known as Mean Squared Error (MSE). Hence, the residual sum of squares reads on its simplest shape:

$$RSS = \sum_{i=1}^N (f(x_i; \theta_j) - y_i)^2 \quad (8)$$

Where our experimental dataset is given by: $Data = [x_1 \ y_1; x_i \ y_i; x_N \ y_N]$; ‘N’ is the number of experimental data pairs (input-output) we have. The data is a matrix of two columns, one for the input and the corresponding output, and N lines, in which lines correspond to one realization of the physical system under investigation. $f(x_i; \theta_j)$ can be “anything,” from a neural network with weights to be adjusted to a polynomial series with coefficients to be adjusted or a dynamical system with parameters to be adjusted in order to achieve minimal error, the latter called parameter estimation or system identification. Furthermore, x_i are the inputs, the same set applied to generate y_i ; θ_j are the model adjustable values (e.g., weights for neural networks, coefficient for regressions and parameters for dynamical system). Some [8] normalizes eq.8 with the standard deviation, however we do not have this measure directly, thus we have chosen to use the “raw” RSS.

Generating data. One issue that our data presents is that it is not abundant: the more data we have the better usually is the parameter estimation process. A second issue is that we just have data for ghrelin in bloodstream, no data for the gastrointestinal tract dynamics (the second issue was handled by fixing some parameters in order to avoid several possible solutions, see table 2, which would have been pointless letting it free). Thus, we need to generate/sample more data (unfortunately, we cannot redo the experiment, and we challenge medical doctors and biologist reading this paper to sample the data we need to enforce the model).

Two pathways can be followed for exploiting the data we have, both tested herein, and giving to a certain extent the same result for our problem: 1) simulate the dynamical system and compare the distance between the experimental sample time and the simulated time, take the closet one; 2) Use another methodology for creating “fake” data, so we have data for any time we need, for the numerical routine. We preferred the latter for allowing more flexibility regarding future changes in the model. We applied a feedforward neural networks to learn the data we have, and replacing them as input for the parameter estimation process.

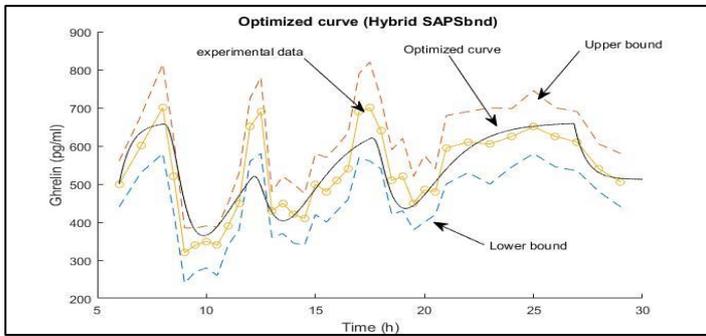


Figure 2: Optimal curve (Hybrid SAPSbnd). The upper and lower bounds are also experimental, being given by: mean +/- Standard Error [3]. See table 6 for acronyms. Source: Authors, (2018).

III.2 METHODOLOGICAL CONSIDERATIONS

We provide an exhaustive parameter estimation, testing several possible combinations of what we have called herein “hybrid” algorithms (global search + local search, cf., Fig. 3); the motivation is gathering the well-known strengths of each technique in one practice, i.e. global search is well-known to explore the search space, whereas local search to converge fast to the closest optimum. After the exhaustive investigation on the model from a parameter estimation perspective, we can conclude that any improvement is no longer an optimization issue, but rather future versions of the model for accounting for missing details; the model presented herein can be called the “minimum/reduced model” keeping in mind a more well-elaborated version is discussed on [1].



Figure 2: Schematic view of our hybrid algorithm. Source: Pires, 2017 [1]

III.3 SIMULATIONS

For solving the dynamical system presented previously numerically (eq.1-7), we preferred our own coding, a Runge-Kutta 4. As we shall see, we have tested several optimization routines; all the optimization methods were borrowed from Matlab, built-in functions, inserted within the scripts employed for accomplishing the simulations reported herein. For the local search, just one method was tested, we have done just one simulation, whereas for the hybrid methods, composed of one stochastic search (Fig. 3), we have done ten simulations and reported the average values for the parameters and the interval of confidence for the optimal values using the Gaussian distribution ($\alpha=5\%$). Some of the codes will be shared on:

<https://www.dropbox.com/sh/8v3kno16u1zwp69/AABWw6TeXW3VzEYLIAHYtrV-a?dl=0>

It was tested several routines, see [1] for comparing, however, we just report the imperative simulations, the least promising results are left for curious readers to get in touch. One

interesting case to report is regarding particle swarm. Unfortunately, due to unknown reasons it did not work well for the problem herein, even after parameter changes; therefore, we shall not report the hybrid algorithms designed. Because our problem is physiological, it is senseless allowing any solution: bounds were set at the parameters. Two ways can be done for bounds: i) using an algorithm based on bounds; ii) creating an external trick. We have tested both; details on the external bounds can be found on [2]. The advantage of external bounds is that we can use unconstrained optimization (generally faster than constrained optimization), whereas for internal bounds we can avoid problems that can happen when we arrive close to the bounds. Just one local search is reported, but we tested several of them: Nelder-Mead Method. The problem with local search is the need to set initial conditions: it was set by hand-picking, which can be cumbersome if we must change the model, or any detail, for future versions of the model. As so, the hybrid methods overcome this detail: but they are surely slower and give more variability on the final solutions.

In the upcoming table, Table 4, we have the algorithms and their outputs. The results are quite similar, with small differences between the methods. For the hybrid methods, due to the first step being stochastic search, we ran it out ten times, and took the average value; for the fitness function, we report an interval of confidence based on a Gaussian distribution ($\alpha=5\%$).

V DISCUSSIONS

The application of soft computing (e.g., genetic algorithm) is not uncommon in biological systems, as we have done herein. Therefore, we show once more numerically the possibility to apply soft computing successfully and hybrid algorithms on ‘parameter estimation’, as an alternative route for classical methods/local search.

V.1 THE NUMERICAL SIMULATIONS

On Table 4, we have the numerical methods applied and their outputs. The methods were divided into: local search and global search. We reported just the interesting results, further results are left as curiosity for interested reader to contact us. The global search was done in the hybrid style: one local search + a global search, see Fig. 3.

Table 4: List of optimization methods and their outputs (see Table 6).

Parameter	Nelder-Mead Method	Hybrid GAIP	Hybrid SAPSbnd
k_{sh}	2.4380 (0.8912)	2.0945	1.9958
β_d	1600 (3.9221 10^{15})	1349.9	1314.7
β_n	1256.1 (1.6407)	1063.1	1314.7
t_{switch}	26.9992 (2694.0)	26.6877	26.8828
γ	1.2788 (0.2459)	1.2553	1.2332
τ_b	38.4919 (-0.0533)	40.6454	42.1076
τ_i	24.0363 (-420.9745)	25.6978	26.5781
τ_d	24.0060 (-2554.7)	24.9550	24.0592
δ	5.0909 10^{-04} (-6.3191)	2.8197e-04	8.3576e-04
r	2.1 ^(FV)	-	-
k_{sj}	2.3 ^(FV)	-	-
k_{jx}	0.71 ^(FV)	-	-
Best (10^j)	6.05527	(5.8962, 5.9508, 6.0054)	(5.8826, 6.0514, 6.2203)

Legend. FV – fixed value. Note. The values between parenthesis are the true values found, before external bound setting.

Source: Authors, (2018).

In the upcoming table, Table 5, we have initial conditions used on the local search.

Table 5: Initial values applied when needed.

k_{sh}	β_d (10^{15})	β_n	t_{switch}	γ	τ_b	τ_l	τ_d	δ
0.9257	1.5851	- 150.361	1273.2	- 0.112	- 0.043	- 254.387	- 254.387	- 3.075

Source: Authors, (2018).

V.2 EFFECTIVENESS OF THE MODELING

Ghrelin has two key dynamics: i) day-night dynamics; ii) long-short term dynamics. The former has to do with the shift of physiological behavior observed around 2 a.m [3], whereas the latter has to do with the double-dynamics observed in ghrelin [12], one in meal-like timescale and the other in terms of bodyweight timescale. In our model, we just concerned about the day-night dynamics; insights for the long-short term dynamics is presented by [2,5]. As we can see from eq.7, we solved the problem by adding a two-state variable, one ghrelin production rate for day, when meals drive the ghrelin production, whereas at night it is internal physiological processes, modeled by a second value for ghrelin. As we can see from Table 4, the value estimated for night is slightly smaller. This can be explained based on the fact that at night our hormonal machinery is reduced (metabolism), which most likely affects also the production of the hunger hormone; see that ghrelin is a pleiotropic hormone, which means that its functions go beyond just food intake control. The half-life of ghrelin in humans is about 240 min [12], which gives us an elimination rate equals about '0,003 min⁻¹' or '0,17 h⁻¹'; we found 1.9958, which is relatively close, the value 0.007 was applied by [13] in mice studies.

Table 6: List of acronyms (algorithms) mentioned herein.

Acronym	Meaning	comment	In Matlab
SAPSbnd	Simulated Annealing Pattern Search Bounded	This algorithm mixtures sa and ps, all bounded search.	Simulannealbnd + patternsearch
GAIP	Genetic Algorithm Internal Point	This algorithm mixtures ga and ip, all unbounded search.	ga + fmincon

Source: Authors, (2018).

V.3 IMPROVING THE MODEL

Remodeling the gastric feedback. The model for gastric feedback we have applied herein is a simplification for the physiology behind. It is true that as the small intestine starts to be excited by nutrient load present in foodstuff, the hormones that control gastric feedback shall be either suppressed or produced, thus we have a positive correlation. However, the true physiology behind, if we want to have a model closer to reality, must be taken into account. It means that we must model the hormones individually, or at least some of them. Ghrelin also was found to control gastric emptying, in an opposite direction, when ghrelin is high, it seems to induce gastric emptying, rather than suppressing, as most of them do.

The "night mode". The "night model", as we see it here and may be found in the literature with other names, is a sequence of hormone changes due night/sleeping period. One example is the dawn phenomenon (cf., [17]). In our model, we have modeled the effect of that on ghrelin production as a "two-state" function (day or night); in fact, we are assuming that the "night mode" is responsible for the decline in ghrelin concentration at night, where there is no meal to explain the fall-off. More interesting modeling would be to take into account "hormones", being it "fake" (a mathematical trick) or real (based on physiological observations); thus, the concentration of this hormone must grow throughout the day and become significant high at night. Some of this fall-off seems to be explained by leptin, that can join independently or as net force on this fall-off of ghrelin during the night.

The production rate. As we can see in Fig. 2, the model fits well on the two meals after breakfast, but fails between breakfast and lunch. It happens because the ghrelin production rate, a constant β , is the same for the whole day. We may need to consider a time-dependent "constant" for ghrelin production; or even consider having different suppression factors for ghrelin as a function of food content, which is not an unknown physiological fact that ghrelin responds differently to different macronutrients.

Optimization methods. We have used several optimization models. We honestly believe that from an optimization perspective, we did more than enough, accordingly any future problem is regarding model improvement. We did not test all the combinations on the "hybrid style", since we have a considerable amount of local and global search techniques to consider. Others were not considered, e.g. evolutionary strategies, except for scientific curiosity, we see no strong reason to elongate further this issue; it seems unlikely that other methods may improve the fitting, if we need it somehow.

The loss/fitness function. One problem with our parameter estimation is that we do not have data for the stomach and small intestine (gastrointestinal tract), from the same experiment with ghrelin. It means that we either must fix the parameters from the gastrointestinal tract, to avoid multiple possible solutions, or we need data for the gastrointestinal tract². To the best of our knowledge, at the current time, there is no paper that would fulfil the last possibility, thus avoiding multiple solutions for the parameter estimation procedure. A possible fitness function would be, which is just an extension of eq.8:

$$RSS = \sum_{i=1}^N (f(x_i; \theta_j) - y_i)^2 + \sum_{i=1}^N (g(x_i; \theta_j) - w_i)^2 + \sum_{i=1}^N (h(x_i; \theta_j) - s_i)^2 \quad (9)$$

Where: $g(x_i; \theta_j)$ is the stomach dynamics, and w_i experimental data, like the one for ghrelin, measured in time; $h(x_i; \theta_j)$ is the dynamics for the small intestine (or any other chosen compartment, e.g. jejunum), and s_i the time dependent experimental data.

V.3 FINAL REMARKS

On this short paper, we have presented a mathematical model for ghrelin dynamics, a hormone now well-known to play a central role on appetite/food intake control. We have confronted the model mathematically with in vivo data via parameter estimation. Notwithstanding the parameter estimation was unable to model precisely the experimental data, most likely due to

² It seems, from personal communication with a nutritionist interested in the model, that such a measure may be physiologically hard to obtain.

physiological details still unclear in the literature, it generated an optimized curve relatively close to the experimental data, leaving promising results for future investigations. As a key future work is obtaining in vivo data for the gastrointestinal tract, by this manner estimating also the parameters relative to the gastrointestinal tract and comparing them with values already found using other methods.

IV ACKNOWLEDGMENTS

This work is a republication of “A hybrid algorithm for parameter estimation of the ghrelin dynamics based on in vivo data” (*Congresso Brasileiro de Inteligência Computacional 2017*): <http://cbic2017.org/papers/cbic-paper-9.pdf>

V REFERENCES

- [1] Pires, J.G.: **Mathematical modeling in energy homeostasis, appetite control and food intake with a special attention to ghrelin**. Dissertation, University of L'Aquila, 2017.
- [2] Cobelli, C., Carson, E.: **Introduction to modeling in physiology and medicine**. Elsevier/Academic Press, Amsterdam (2008).
- [3] Cummings, D.E., Purnell, J.Q., Frayo, R.S, Schmidova, K., Wisse, B.E., Castracane D.S.: **A Preprandial Rise in Plasma Ghrelin Levels Suggests Role in Meal Initiation in Humans**. Rapid Publication. Diabetes. 50(8),1714-9 (2001).
- [4] Pires, J.G., Borri, A., De Gaetano, A., Manes, C., Palumbo, P.: **A short-term dynamical model for ghrelin**. Paper presented at 20th World Congress of the International Federation of Automatic Control, Toulouse, France, 9-14 July 2017.
- [5] Cummings, D.E., Foster-Schubert, K.E., Overduin, J.: **Ghrelin and energy balance: Focus on current controversies**. Curr Drug Targets. 6, 153–169 (2005).
- [6] Fox, S.I.: **Human Physiology**. Twelfth edition. McGraw Hill, New York. (2011).
- [7] Karasu, S.R., Karasu, T.B.: **The Gravity of Weight: a clinical guide to Weight Loss and Maintenance**. American psychiatric Publishing, Inc. (2010).
- [8] Roman, H., and Paolo V.: **Parameter Estimation**. In: Carson, E., Cobelli, C. (eds) Modelling Methodology for Physiology and Medicine, pp. 107-151, Academic Press, San Diego (2001).
- [9] Jacquier, M.: **Mathematical modeling of the hormonal regulation of food intake and body weight Applications to caloric restriction and leptin resistance**. Dissertation, Université Claude Bernard Lyon 1. (2016).
- [10] Pattaranit, R., van den Berg. HA.: **Mathematical models of energy homeostasis**. Review. J. R. Soc. Interface 5, 1119–1135 (2008).
- [11] Tam, J., Fukumura, D., Jain, R.K.: **A mathematical model of murine metabolic regulation by leptin: energy balance and defense of a stable body weight**. Cell Metab. 9(1), 52–63 (2009).
- [12] Cummings, D.E., Weigle, D.S., Frayo, R.S., et al.: **Plasma Ghrelin levels after diet-induced weight loss or gastric bypass surgery**. New England Journal of Medicine. 346(21), 1623–1630 (2002).
- [13] Müller, T.D., et al.: **Ghrelin**. Minireview. Molecular Metabolism. 4, 437-460 (2015).
- [14] Jacquier, M., Soula, H., Crauste, F.: **A mathematical model of leptin resistance**. Mathemati-cal biosciences. 267:10–23 (2015).
- [15] World Obesity Federation: **World Obesity**. <http://www.worldobesity.org/data/map/trend-maps-boys>. Accessed on 21/07/2017.
- [16] Liddle, R.A., Morita. E.T., Conrad, C.K., Williams, J.A.: **Regulation of gastric emptying in humans by cholecystokinin**. 77(3), 992–996 1986.
- [17] Ling, S.H., San, P.P. Nguyen, H.T.: **Hypoglycemia Detection for Insulin-dependent Diabetes Mellitus: Evolved Fuzzy Inference System Approach**. In: Lam. H.K, Ling, S.H. Ngu-yen, H.T. (eds.) Computational Intelligence and its applications: Evolutionary Computation, Fuzzy Logic, Neural Network and Support Vector Machine Techniques, 61-85. Imperial College Press, London (2012).
- [18] Barnabei, M. **A mathematical model of meal absorption**. Università degli Studi dell'Aquila Ingegneria: L'Aquila, 2017.